



### Quick word about me

- Postdoc Researcher at ISIR-CNRS (Sorbonne University)
- PhD from Paris-Saclay University (LISN-CNRS lab)
- Research topic: Multilingual Large Language Models
- More about me: <a href="https://paullerner.github.io">https://paullerner.github.io</a>
- Contact: <a href="mailto:lerner@isir.upmc.fr">lerner@isir.upmc.fr</a>



### **Acknowledgements**

### This class directly builds upon:

- **Jurafsky, D., & Martin, J. H.** (2024). Speech and Language Processing: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition with Language Models (3rd éd.).
- **Eisenstein, J.** (2019). Natural Language Processing. 587.
- **Yejin Choi**. (Winter 2024). CSE 447/517: Natural Language Processing (University of Washington Paul G. Allen School of Computer Science & Engineering)
- **Noah Smith**. (Winter 2023). CSE 447/517: Natural Language Processing (University of Washington Paul G. Allen School of Computer Science & Engineering)
- Benoît Sagot. (2023-2024). Apprendre les langues aux machines (Collège de France)
- Chris Manning. (Spring 2024). Stanford CS224N: Natural Language Processing with Deep Learning
- Classes where I was/am Teacher Assistant:
  - Christopher Kermorvant. Machine Learning for Natural Language Processing (ENSAE)
  - François Landes and Kim Gerdes. Introduction to Machine Learning and NLP (Paris-Saclay)

### Also inspired by:

- My PhD thesis: Répondre aux questions visuelles à propos d'entités nommées (2023)
- Noah Smith (2023): Introduction to Sequence Models (LxMLS)
- **Kyunghyun Cho**: Transformers and Large Pretrained Models (LxMLS 2023), Neural Machine Translation (ALPS 2021)
- My former PhD advisors Olivier Ferret and Camille Guinaudeau and postdoc advisor François Yvon
- My former colleagues at LISN





### **Program for this semester**

- This morning (September 29th): What is NLP? What is a word? How can you classify a text made of words?
- Then: Practical Work 1
- Next week (October 9th): How do you get a sense of a word?
- Then: Practical Work 2
- October 23rd: N-gram and Neural Language Models
- Then: Practical Work 1/2 extra
- November 4th: Practical Work 3 (2 sessions)





### **Program for this semester**

- November 10th: Neural Network architectures used in Large Language Models:
  - Recurrent Neural Networks
  - Attention Mechanism
- Then: Transformers pretraining and fine-tuning
- November 20th: Practical Work 4 (2 sessions)
- November 27th: Practical Work 5 (2 sessions)



### **Program for this semester**

- December 4th:
  - Ethical, social, and environmental issues
  - alignment: reinforcement learning from human feedback (RLHF)
  - other things happening in NLP research at the moment
- Then: Practical Work 6
- Practical Works → individual evaluation 50%
- Individual Final sitting Exam 50%



### **Background**

- Assumes basics in Machine Learning, Python, and Linear Algebra
  - Good exercices /cheatsheet "Day 0: Basic Tutorials" of http://lxmls.it.pt/2023/documents/LxMLS\_guide\_2023.pdf
- Recommended readings:
  - Daniel Jurafsky and James H. Martin. 2025. Speech and Language Processing: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition with Language Models, 3rd edition. Online manuscript released January 12, 2025. <a href="https://web.stanford.edu/~jurafsky/slp3">https://web.stanford.edu/~jurafsky/slp3</a>
  - Eisenstein, J. (2019). Natural Language Processing.
     <a href="https://nlp.cs.princeton.edu/cos484-sp21/readings/eisenstein-nl-p-notes.pdf">https://nlp.cs.princeton.edu/cos484-sp21/readings/eisenstein-nl-p-notes.pdf</a>

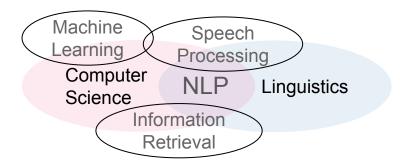
# **Natural Language Processing (NLP)**

Computer NLP Linguistics

- Intersection of Computer Science and Linguistics:
  - Distributional Semantics: sense of a word from its context (next class)
  - Computational Linguistics, Computational Morphology, etc.: study of humans: how do we speak? how do we organize lexicon?



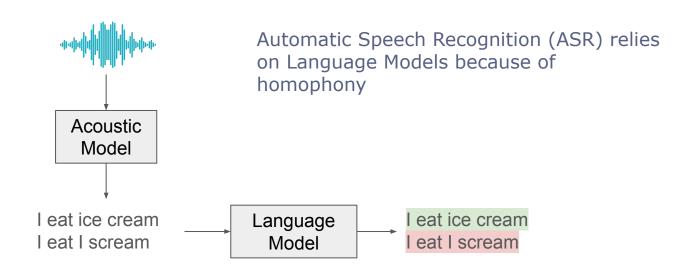
# **Natural Language Processing (NLP)**



- Close to Speech Processing (Automatic Speech Recognition etc.)
- Close to Information Retrieval (Search engines like Google)
- Driven by Statistical/Machine Learning methods since the 90s
- Driven by Deep Learning since 2010s

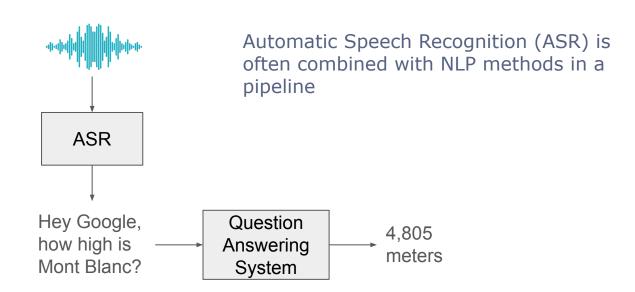


### **Speech and Language Processing**





# **Speech and Language Processing**



# **Speech and Language Processing**



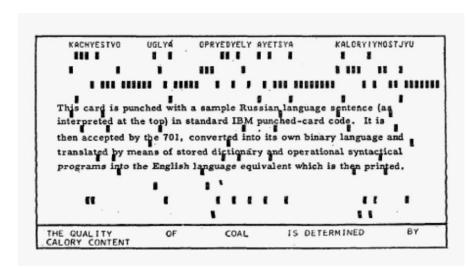
Recently moving towards integrated, multimodal end-to-end models

### What is scientific research?

- General goal: Pushing the limits of our knowledge
- Incrementally! Find a limit/caveat in existing method and solve it!
- For example: lack of parallelization in Recurrent Neural Networks →
   Transformers (Vaswani et al. 2017)
- "Vaswani et al. 2017": a single publication that was **submitted** to a conference, **reviewed** by scientists, then **reproduced**: **research**!= **science**
- Most of methods in this class were published less than 15 years ago



# **NLP applications: Machine Translation**



Georgetown-IBM experiment 1954

- Machine Translation is the first NLP application
- Google Translate supports 243 languages





### **NLP applications: Machine Translation**

### Ubiquitous on the web and social media





Fun new paper led by <code>@IngoZiegler</code> and <code>@akoksal\_</code> that shows how we can use retrieval augmentation to create high-quality supervised fine tuning data. All you need to do is write a few examples that demonstrate the task.

#### À l'origine en anglais et traduit par Google

Un nouvel article intéressant dirigé par @IngoZiegler et @akoksal\_ qui montre comment nous pouvons utiliser l'augmentation de la récupération pour créer des données de réglage fin supervisées de haute qualité. Tout ce que vous avez à faire est d'écrire quelques exemples qui illustrent la tâche.



Part 1

# Is this spam?

Dear Paul

As per our discussions, I hereby confirm your teaching of the following courses for the 2526 academic year:

- 1. Natural Language Processing: PGE4 INI for S1 (24 hours)
- Natural Language Processing: PGE4 ALT for S2 (24 hours)

Best regards, Anuradha

#### **LIDL™**

Offre Exclusive - Clients Sélectionnés

#### **Coffret Makita pour**

Félicitations ! Vous avez été sélectionné(e) pour recevoir un Coffret Makita Professionnel de 108 pièces.

Cette offre est **strictement limitée** aux clients tirés au sort. Profitez-en dès maintenant avant la date limite.

ID Coupon: MAK845652

Date limite: 8-30-2025



Je réclame mon Coffret



### Who wrote which Federalist Papers?

1787-8: essays anonymously written by:

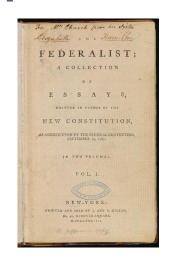
Alexander Hamilton, James Madison, and John Jay

to convince New York to ratify U.S Constitution

Authorship of 12 of the letters unclear between:







Alexander Hamilton

James Madison

1963: solved by Mosteller and Wallace using Bayesian methods



# Positive or negative movie review?



unbelievably disappointing



Full of zany characters and richly applied satire, and some great plot twists



this is the greatest screwball comedy ever filmed



It was pathetic. The worst part about it was the boxing scenes.



### What is the subject of this article?

### MEDLINE Article

### **MeSH Subject Category Hierarchy**





Antogonists and Inhibitors

**Blood Supply** 

Chemistry

**Drug Therapy** 

**Embryology** 

Epidemiology

. . .

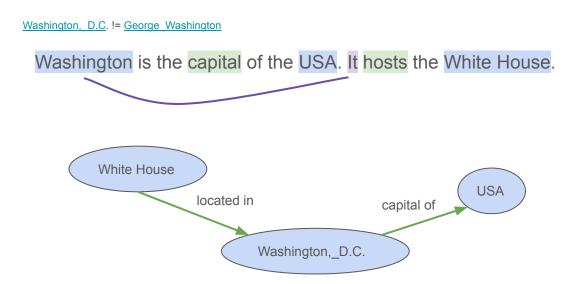


### **Text Classification**

- Assigning subject categories, topics, or genres
- Spam detection
- Authorship identification (who wrote this?)
- Language Identification (is this Portuguese?)
- Sentiment analysis



### **NLP applications: Information Extraction**

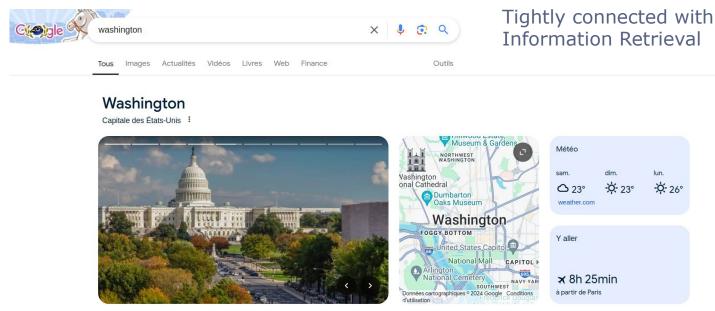


- From unstructured text to knowledge graphs
- Named Entity Recognition
- Named Entity
   Disambiguation
- Coreference resolution
- Relation Extraction





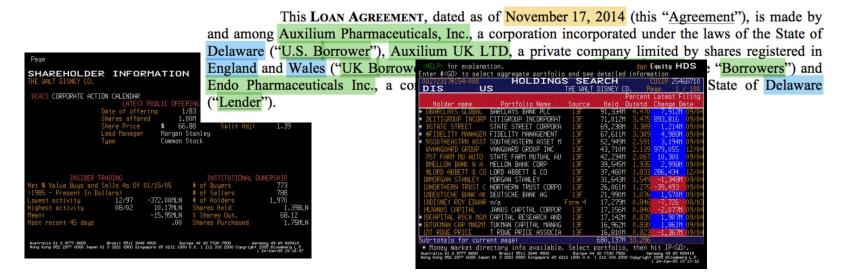
### **NLP applications: Information Extraction**



### **NLP applications: Information Extraction**

Not only for advancing human knowledge

#### **LOAN AGREEMENT**







### **NLP** applications: chatbots

- Task-oriented like Siri/Alexa or chitchat like ChatGPT (OpenAI)
- Moving from a complicated pipeline (ASR, Information Extraction, Information Retrieval) to end-to-end language modeling









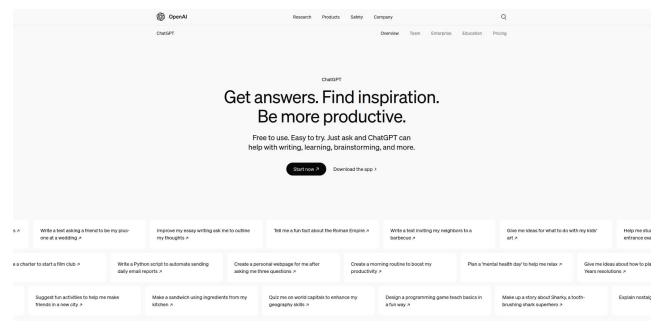








### **NLP** applications: chatbots



### 32 lines of python code

```
from transformers import AutoModelForCausalLM, AutoTokenizer, BitsAndBytesConfig
def pipeline(text, model, tokenizer):
    messages = [
       {"role": "user", "content": text}
   inputs = tokenizer.apply_chat_template(messages, return_dict=True, tokenize=True, return_tensors="pt", add_generation_prompt=True)
   for k, v in inputs.items():
        inputs[k] = v.cuda()
   input_length = inputs["input_ids"].shape[1]
    output = model.generate(**inputs, max_new_tokens=128)
    output = tokenizer.batch_decode(output[:, input_length:], skip_special_tokens=True, clean_up_tokenization_spaces=True)
   return output
def user_loop(model, tokenizer):
    while True:
        answer = input(f">>> ").strip()
        output = pipeline(answer, model, tokenizer)[0]
        print(f"{output}\n")
def main():
    model_name = "google/gemma-2-2b-it"
    model = AutoModelForCausalLM.from_pretrained(
        model_name,
        device_map="auto".
       token=True,
        quantization_config=BitsAndBytesConfig(load_in_4bit=True)
    tokenizer = AutoTokenizer.from_pretrained(model_name)
 user_loop(model, tokenizer)
```



```
>>> what is distributional semantics?
## Distributional Semantics: Understanding Words in Context

Distributional semantics is a branch of natural language processing (NLP) that focuses on the **relationships between words and their meaning based on their co-occurrence in a large corpus of text**.

Think of it like this: instead of focusing on individual words and their exact definitions, distributional semantics analyzes how words are used in context.

**Here's a breakdown:**

* **Words are not isolated:** They are part of a larger network of words and phrases.

* **Meaning is derived from context:** The meaning of a word is determined by how it is
```

```
>>> I'm teaching an NLP class at the aivancity AI school, any advices?
That's awesome! Teaching NLP is a fantastic way to share the power of AI with the next generation. Here's some advice to make your class engaging and impactful:

**1. Know Your Audience:**

* **Beginner or Advanced?** Are you targeting absolute beginners or those with some prior knowledge? Tailor your content and pace accordingly.

* **AI Enthusiasts vs. General Interest:** Are you aiming for a more technical audience or those with a broader interest in AI?

* **Learning Style:** Consider how your students learn best (visual, auditory, kinesthetic). Incorporate divers e teaching methods.
```

>>> you're speaking live to students of the aivancity AI school, introduce yourself
Hello everyone! W I'm Gemma, an AI assistant here to help you learn and explore the fascinating world of AI.

I'm excited to be speaking with you today at Aivancity AI School. I've been trained on a massive dataset of te xt and code, which allows me to understand and generate human-like text.

What are you working on today? Do you have any questions about AI concepts, or are you working on a specific project? I'm here to help!

Let's dive into the world of AI together! 🤖





# **Break for questions and "appel"**



### What is a word?

- Open question in phonology vs. morphology
- Inflection: is brother!= brothers?
- Compounding: is motorbike == motor + bike?
- Multi-word expressions: mother in law == 1 or 3 words?
- Homonymy: is chair (furniture) != chair (person)?
- Orthography: is modeling != modelling?

### **NLP** deals with orthographic words

- "My brother is sitting on a chair" →
  ['My', 'brother', 'is', 'sitting', 'on', 'a', 'chair']
  (tokenization: sequence of tokens)
- Inflection (brother vs brothers): usually not modeled
- Compounding (motorbike vs motor + bike): usually not modeled
- Multi-word expressions (mother in law): usually not modeled
- Homonymy (chair [furniture] vs chair [person]): usually modeled after sharing an initial representation
- Orthography: 'modeling' != 'modelling'



### **Issues in Tokenization**

- Can't just blindly remove punctuation:
  - o m.p.h., Ph.D., AT&T, cap'n
  - prices (\$45.55)
  - dates (01/02/06)
  - URLs (http://www.stanford.edu)
  - hashtags (#nlproc)
  - email addresses (someone@cs.colorado.edu)
- Clitic: a word that doesn't stand on its own
  - o "are" in we're, French "je" in j'ai, "le" in l'honneur



# **Using regular expressions**

```
>>> text = 'That U.S.A. poster-print costs $12.40...'
>>> pattern = r'''(?x) # set flag to allow verbose regexps
                         # abbreviations, e.g. U.S.A.
    (?:[A-Z]\.)+
# words with optional internal hyphens
... | \$?\d+(?:\.\d+)?\%? # currency, percentages, e.g. $12.40, 82%
... | \.\.\.
                       # ellipsis
   | [][.,;"'?():_'-] # these are separate tokens; includes ], [
>>> nltk.regexp_tokenize(text, pattern)
['That', 'U.S.A.', 'poster-print', 'costs', '$12.40', '...
```

AN

### Why regular expressions?

- A formal language for specifying text strings
- How can we search for mentions of these cute animals in text?
  - woodchuck
  - woodchucks
  - Woodchuck
  - Woodchucks
  - Groundhog
  - groundhogs



# **Regular Expressions: Disjunctions**

Letters inside square brackets []

Pattern	Matches
[wW]oodchuck	Woodchuck, woodchuck
[1234567890]	Any one digit

Ranges using the dash [A-Z]

COPICITION LOLD

Pattern	Matches	
[A-Z]	An upper case letter	Drenched Blossoms
[a-z]	A lower case letter	my beans were impatient
[0-9]	A single digit	Chapter 1: Down the Rabbit Hole

## **Regular Expressions: More Disjunctions**

- Groundhog is another name for woodchuck!
- The pipe symbol | for disjunction

Pattern	Matches
groundhog   woodchuck	woodchuck
yours   mine	yours
a   b   c	= [abc]
[gG]roundhog [Ww]oodchuck	Woodchuck



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## Regular Expressions: Convenient aliases

Pattern	Expansion	Matches	Examples
\d	[0-9]	Any digit	Fahreneit <u>4</u> 51
\D	[^0-9]	Any non-digit	Blue Moon
\w	[a-ZA-Z0-9_]	Any alphanumeric or _	<u>D</u> aiyu
/W	[^\w]	Not alphanumeric or _	Look!
\s	$[ \r\t\n\f]$	Whitespace (space, tab)	Look _ up
\S	[^\s]	Not whitespace	<u>L</u> ook up



## Wildcards, optionality, repetition: .? \* +

Pattern	Matches	Examples
beg.n	Any char	<pre>begin begun beg3n beg n</pre>
woodchucks?	Optional s	woodchucks woodchucks
to*	0 or more of previous char	t to too tooo
to+	1 or more of previous char	<u>to too tooo</u> t <u>oooo</u>



Stephen C Kleene

Kleene \*, Kleene + aivancity PARIS-CACHAN

## A note about Python regular expressions

- Regex and Python both use backslash "\" for special characters. You must type extra backslashes!
  - "\\d+" to search for 1 or more digits
  - "\n" in Python means the "newline" character, not a "slash" followed by an "n". Need "\n" for two characters.
- Instead: use Python's raw string notation for regex:
  - o r"[tT]he"
  - r"\d+" matches one or more digits



#### **Strings of characters**

- Note in python: there are no characters, only strings!
- "foo" is a string
- "foo"[0] is a string ("f")
- "foo"[0][0] is a string ("f")

## The iterative process of writing regex's

•Find me all instances of the word "the" in a text.

```
the
    Misses capitalized examples

[tT] he
    Incorrectly returns other or Theology
```

Good tool to learn <a href="https://regex101.com/">https://regex101.com/</a>

\W[tT]he\W



## Tokenization in languages without spaces

- Many languages (like Chinese, Japanese, Thai) don't use spaces to separate words!
- How do we decide where the token boundaries should be?



#### Word tokenization in Chinese

- Chinese words are composed of characters called "hanzi" (or sometimes just "zi")
- Each one represents a meaning unit called a morpheme.
- Each word has on average 2.4 of them.
- But deciding what counts as a word is complex and not agreed upon.



#### How to do word tokenization in Chinese?

- ●姚明进入总决赛 "Yao Ming reaches the finals"
- •3 words?
- YaoMing reaches finals
- •5 words?
- ●姚 明 进入 总 决赛
- Yao Ming reaches overall finals
- ●7 characters? (don't use words at all): ●姚 明 进 入 总 决 狠
- Yao Ming enter enter overall decision game



## Zipf's Law

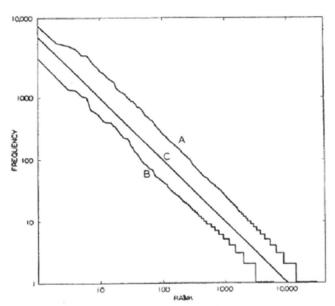


Fig. 2-1. The rank-frequency distribution of words. (A) The James Joyce data; (B) the Eldridge data; (C) ideal curve with slope of negative unity.

Zipf (1949) found that, when counting the frequencies of all words in a Joyce's Ulysses (**260,430 words**), that:

- the 10th most frequent word occurred 2,653 times
- the 100th 265 times, or 10 times less
- the **1000th 26** times, or 100 times less

In other words, the frequency f(w) of a word w is inversely proportional to its rank k:  $f(w) \propto 1/k$ 

or 
$$f(w) \times k = \text{constant}$$

#### Zipf's Law

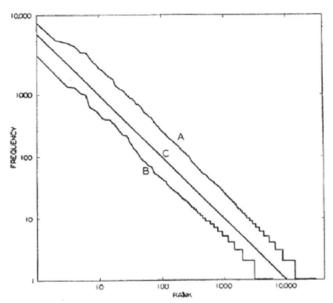
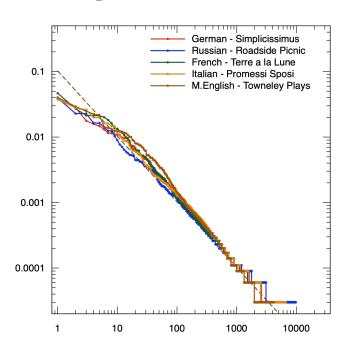


Fig. 2-1. The rank-frequency distribution of words. (A) The James Joyce data; (B) the Eldridge data; (C) ideal curve with slope of negative unity.

- The frequency f(w) of a word w is inversely proportional to its rank k:  $f(w) \propto 1/k$
- The distribution of words frequencies have a very long tail: some words are very frequent other appear only once in the whole training corpus

## **Zipf's Law**



- The frequency f(w) of a word w is inversely proportional to its rank k:  $f(w) \propto 1/k$
- The distribution of words frequencies have a very long tail: some words are very frequent other appear only once in the whole training corpus
- This empirical law was verified in most languages of the world, it's one of the canonical laws of computational linguistics

#### Open vs. closed vocabulary

- Training a classifier → mostly fine to have a fixed vocabulary of *V* words.
   Top-k ones will cover vast majority of corpus, why?
- What about for a generative model?
- For a multilingual model (e.g. English-Chinese)?
- Use a fixed vocabulary of V' subwords that can be combined into words
- "open" vocabulary but still a finite set of tokens



## Byte Pair Encoding (BPE) token learner

- Let vocabulary be the set of all individual characters
- = {A, B, C, D,..., a, b, c, d....}
- Repeat:
  - Choose the two symbols that are most frequently adjacent in the training corpus (say 'A', 'B')
  - Add a new merged symbol 'AB' to the vocabulary
  - Replace every adjacent 'A' 'B' in the corpus with 'AB'.
- Until k merges have been done.



## **BPE** token learner algorithm

function BYTE-PAIR ENCODING(strings C, number of merges k) returns vocab V

```
V \leftarrow all unique characters in C # initial set of tokens is characters

for i = 1 to k do # merge tokens til k times

t_L, t_R \leftarrow Most frequent pair of adjacent tokens in C

t_{NEW} \leftarrow t_L + t_R # make new token by concatenating

V \leftarrow V + t_{NEW} # update the vocabulary

Replace each occurrence of t_L, t_R in C with t_{NEW} # and update the corpus

return V
```

## Byte Pair Encoding (BPE) Addendum

- Most subword algorithms are run inside space-separated tokens.
- So we commonly first add a special begin-of-word symbol 'Ġ' before space in training corpus
- Next, separate into letters.



Original (very fascinating 22) corpus:

low low low low lowest lowest newer newer newer newer newer wider wider wider new new

Add begin-of-word tokens, resulting in this vocabulary:

Ġlowestnrid



#### corpus

```
5 Ġ l o w
2 Ġ l o w e s t
6 Ġ n e w e r
3 Ġ w i d e r
2 Ġ n e w
```

#### vocabulary

Ġlowestnrid

Merge e r to er

#### corpus

```
5 Ġ l o w
2 Ġ l o w e s t
6 Ġ n e w er
3 Ġ w i d er
2 Ġ n e w
```

#### vocabulary

```
Ġ l o w e s t n r i d
er
```

#### Merge G n to Gn

#### corpus

```
5 Ġ 1 o w
```

- 2 Ġ l o w e s t
- 6 Ġn e w er
- 3 Ġ w i d er
- 2 Ġn e w

#### vocabulary

Ġlowestnrid erĠn

## Merge Gn e to Gne

#### corpus

```
5 Ġ 1 o w
```

- 2 Ġ l o w e s t
- 6 Ġne w er
- 3 Ġ w i d er
- 2 Ġne w

#### vocabulary

```
Ġlowestnrid
erĠnĠne
```

The next merges are:

merge	vocabulary
•	Ġ l o w e s t n r i d er Ġn Ġne Ġnew
(Ġ, 1)	Ġ l o w e s t n r i d er Ġn Ġne Ġnew Ġl
(Ġ1, o)	Ġ l o w e s t n r i d er Ġn Ġne Ġnew Ġl Ġlo
(Ġlo, w)	Ġ l o w e s t n r i d er Ġn Ġne Ġnew Ġl Ġlo Ġlow
(Ġnew, er)	Ġ l o w e s t n r i d er Ġn Ġne Ġnew Ġl Ġlo Ġlow Ġnewer

#### **BPE token segmenter algorithm**

- On the test data, run each merge learned from the training data:
  - Greedily
  - In the order we learned them.
  - (test frequencies don't play a role)
- So: merge every e r to er, then merge Ġ n to Ġn, etc.
- Result:
  - Test set "Ġ n e w e r" would be tokenized as a full word
  - Test set "Ġ I o w e r" would be two tokens: "Ġlow er"

#### **Text Classification**

- Assigning subject categories, topics, or genres
- Spam detection
- Authorship identification (who wrote this?)
- Language Identification (is this Portuguese?)
- Sentiment analysis

#### **Text Classification: definition**

## Input:

- a document d
- $\circ$  a fixed set of classes  $C = \{c_1, c_2, ..., c_j\}$

Output: a predicted class  $c \in C$ 

## Classification Method: Supervised Machine Learning

#### Input:

- a document d
- $\circ$  a fixed set of classes  $C = \{c_1, c_2, ..., c_j\}$
- $\circ$  A training set of m hand-labeled documents  $(d_1, c_1), \dots, (d_m, c_m)$

#### Output:

 $\circ$  a learned classifier  $\gamma:d\to c$ 

$$c_{MAP} = \operatorname{argmax} P(c \mid d)$$

 $c \in C$ 



## **Bayes' Rule**

For a document d and a class C

$$P(c \mid d) = \frac{P(d \mid c)P(c)}{P(d)}$$

## Naive Bayes Classifier (I)

$$c_{MAP} = \operatorname*{argmax} P(c \mid d)$$

MAP is "maximum a posteriori" = most likely class

$$= \underset{c \in C}{\operatorname{argmax}} \frac{P(d \mid c)P(c)}{P(d)}$$

**Bayes Rule** 

$$= \operatorname*{argmax} P(d \mid c) P(c)$$



## Naive Bayes Classifier (II)

$$c_{MAP} = \underset{c \in C}{\operatorname{argmax}} P(d \mid c) P(c)$$

= 
$$\underset{c \in C}{\operatorname{argmax}} P(x_1, x_2, \dots, x_n \mid c) P(c)$$
 represented as features x1..xn

Document d

## Naive Bayes Classifier (III)

$$c_{MAP} = \underset{c \in C}{\operatorname{argmax}} P(x_1, x_2, \dots, x_n \mid c) P(c)$$

 $O(|X|^n \bullet |C|)$  parameters

How often does this class occur?

Could only be estimated if a very, very large number of training examples was available.

We can just count the relative frequencies in a corpus



Part 3

## **Multinomial Naive Bayes Independence Assumptions**

$$P(x_1, x_2, ..., x_n | c)$$

Bag of Words/Naive Bayes assumption: Assume position doesn't matter

**Conditional Independence**: Assume the feature probabilities  $P(x_i | c_i)$  are independent given the class c.

$$P(x_1,...,x_n \mid c) = P(x_1 \mid c) \bullet P(x_2 \mid c) \bullet P(x_3 \mid c) \bullet ... \bullet P(x_n \mid c)$$
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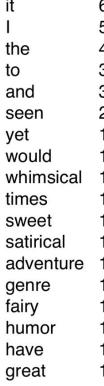
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#### The Bag of Words Representation

I love this movie! It's sweet, but with satirical humor. The dialogue is great and the adventure scenes are fun... It manages to be whimsical and romantic while laughing at the conventions of the fairy tale genre. I would recommend it to just about anyone. I've seen it several times, and I'm always happy to see it again whenever I have a friend who hasn't seen it yet!







#### **Applying Multinomial Naive Bayes Classifiers** to Text Classification

positions ← all word positions in test document

$$c_{NB} = \underset{c_{j} \in C}{\operatorname{argmax}} P(c_{j}) \prod_{i \in positions} P(x_{i} \mid c_{j})$$

## **Problems with multiplying lots of probs**

There's a problem with this:

$$c_{NB} = \underset{c_{j} \in C}{\operatorname{argmax}} P(c_{j}) \prod_{i \in positions} P(x_{i} \mid c_{j})$$

Multiplying lots of probabilities can result in floating-point underflow! .0006 \* .0007 \* .0009 \* .01 \* .5 \* .000008....

Idea: Use logs, because log(ab) = log(a) + log(b)

We'll sum logs of probabilities instead of multiplying probabilities!

## We actually do everything in log space

Instead of this: 
$$c_{NB} = \underset{c_j \in C}{\operatorname{argmax}} P(c_j) \prod_{i \in positions} P(x_i \mid c_j)$$

This: 
$$c_{\text{NB}} = \operatorname*{argmax}_{c_j \in C} \left[ \log P(c_j) + \sum_{i \in \text{positions}} \log P(x_i | c_j) \right]$$

Note: Taking log doesn't change the ranking of classes!
The class with highest probability also has highest log probability!

## **Learning the Multinomial Naive Bayes Model**

First attempt: maximum likelihood estimates

- o simply use the frequencies in the data
- See Eisenstein for proof that it maximizes likelihood

$$\widehat{P}(c_j) = \frac{N_{c_j}}{N_{total}}$$

$$\hat{P}(w_i | c_j) = \frac{count(w_i, c_j)}{\sum count(w, c_j)}$$

fraction of times word  $w_i$  appears among all words in class  $c_i$ 



#### **Problem with Maximum Likelihood**

•What if we have seen no training documents with the word *fantastic* and classified in the topic **positive** (*thumbs-up*)?

$$\hat{P}(\text{"fantastic" | positive}) = \frac{count(\text{"fantastic", positive})}{\sum_{w \in V} count(w, \text{positive})} = 0$$

•Zero probabilities cannot be conditioned away, no matter the other evidence!

$$c_{MAP} = \operatorname{argmax}_{c} \hat{P}(c) \prod_{i} \hat{P}(x_{i} \mid c)$$



## Laplace (add-1) smoothing for Naïve Bayes

$$\hat{P}(w_i \mid c) = \frac{count(w_i, c) + 1}{\sum_{w \in V} (count(w, c)) + 1}$$

$$= \frac{count(w_i, c) + 1}{\sum_{w \in V} count(w, c) + |V|}$$



## **Multinomial Naïve Bayes: Learning**

From training corpus, extract *Vocabulary* 

# Calculate $P(c_j)$ terms • For each $c_j$ in C do

 $docs_i \leftarrow \text{ all docs with class } = c_i$ 

$$P(c_j) \leftarrow \frac{|docs_j|}{|total \# documents|}$$

- Calculate P(w<sub>k</sub> | c<sub>j</sub>) terms
   Text<sub>j</sub> ← single doc containing all docs<sub>j</sub>
   For each word w<sub>k</sub> in Vocabulary  $n_k \leftarrow \#$  of occurrences of  $w_k$  in  $Text_i$

$$P(w_k \mid c_j) \leftarrow \frac{n_k + \alpha}{n + \alpha \mid Vocabulary \mid}$$



#### **Bias-variance tradeoff**

- If  $\alpha$  is large  $\rightarrow$  uniform distribution  $\bullet$   $\rightarrow$  underfit training data
  - high bias
  - low variance
- $\circ$  if  $\alpha$  is small  $\rightarrow$  overfit training data
  - high variance
  - low bias

- Calculate  $P(w_k \mid c_j)$  terms
  - Text<sub>j</sub> ← single doc containing all docs<sub>j</sub>
     For each word w<sub>k</sub> in Vocabulary
  - For each word  $w_k$  in *Vocabulary*  $n_k \leftarrow \#$  of occurrences of  $w_k$  in  $Text_j$

$$P(w_k \mid c_j) \leftarrow \frac{n_k + \alpha}{n + \alpha \mid Vocabulary \mid}$$



## Let's do a worked sentiment example!

	Cat	Documents
Training	-	just plain boring
	-	entirely predictable and lacks energy
	-	no surprises and very few laughs
	+	very powerful
	+	the most fun film of the summer
Test	?	predictable with no fun

## A worked sentiment example with add-1 smoothing

	Cat	Documents
Training	-	just plain boring
	-	entirely predictable and lacks energy
	-	no surprises and very few laughs
	+	very powerful
	+	the most fun film of the summer
Test	?	predictable with no fun

## 3. Likelihoods from training: $p(w_i|c) = \frac{count(w_i,c) + 1}{(\sum_{w \in V} count(w,c)) + |V|}$

$$p(w_i|c) = \frac{count(w_i, c) + 1}{(\sum_{w \in V} count(w, c)) + |V|}$$

$$P(\text{``predictable''}|-) = \frac{1+1}{14+20} \qquad P(\text{``predictable''}|+) = \frac{0+1}{9+20}$$

$$P(\text{``no''}|-) = \frac{1+1}{14+20} \qquad P(\text{``no''}|+) = \frac{0+1}{9+20}$$

$$P(\text{``fun''}|-) = \frac{0+1}{14+20} \qquad P(\text{``fun''}|+) = \frac{1+1}{9+20}$$

$$P(\text{``fun''}|-) = \frac{0+1}{14+20} \qquad P(\text{``fun''}|+) = \frac{1+1}{9+20}$$

#### 1. Prior from training:

$$\widehat{P}(c_j) = \frac{N_{c_j}}{N_{total}} \qquad P(-) = \frac{3}{5}$$

$$P(+) = \frac{2}{5}$$

#### 2. Drop "with"

#### 4. Scoring the test set:

$$P(-)P(S|-) = \frac{3}{5} \times \frac{2 \times 2 \times 1}{34^3} = 6.1 \times 10^{-5}$$

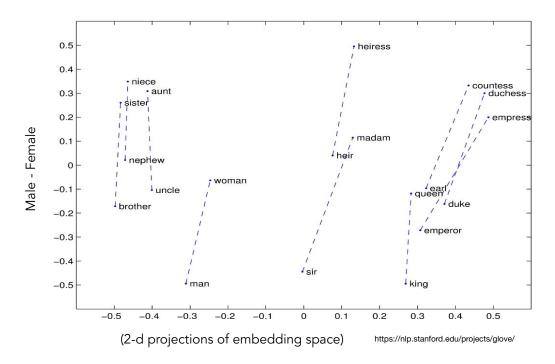
$$P(+)P(S|+) = \frac{2}{5} \times \frac{1 \times 1 \times 2}{20^3} = 3.2 \times 10^{-5}$$

#### **In Summary**

- NLP = research field at the intersection of Computer Science and Linguistics
- NLP = Many industrial applications, from Machine Translation to chatbots like ChatGPT or Information Extraction
- Token = essential unit of NLP: words, subwords, or characters
- Can count token occurrences in texts ("bag of words") to classify them



#### **Next class: distributional semantics**







## Is this spam?

Dear Paul As per our discussions, I hereby confirm your teaching of the following courses for the 2526

- Natural Language Processing: PGE4 INI for S1 (24 hours)
- Natural Language Processing: PGE4 ALT for S2 (24 hours)

Best regards, Anuradha

academic year:

Dear Dr. Lerner,

I'm , a representative at .

We provide three styles of podcast services, designed to enhance the visibility of your work:

These services come with associated production costs, starting at £1,584 for a single podcast or £4,514 for a podcast series, ideal for storytelling across three or more episodes.



#### **Exam**

- The exam will last 2 hours
- Written exam, no documents authorized
- 6/20 points on class questions ("What is X")
- 11/20 points on diverse problems
  - similar to the practical works but by hand
  - or code completion/analysis
  - or disguised class questions ("Alice wants something, how can she do it",
     "Bob did X, what did he do wrong")
- 3/20 points on open question

